

# COMPUTATIONAL INTELLIGENCE

September 2016 – November 2016

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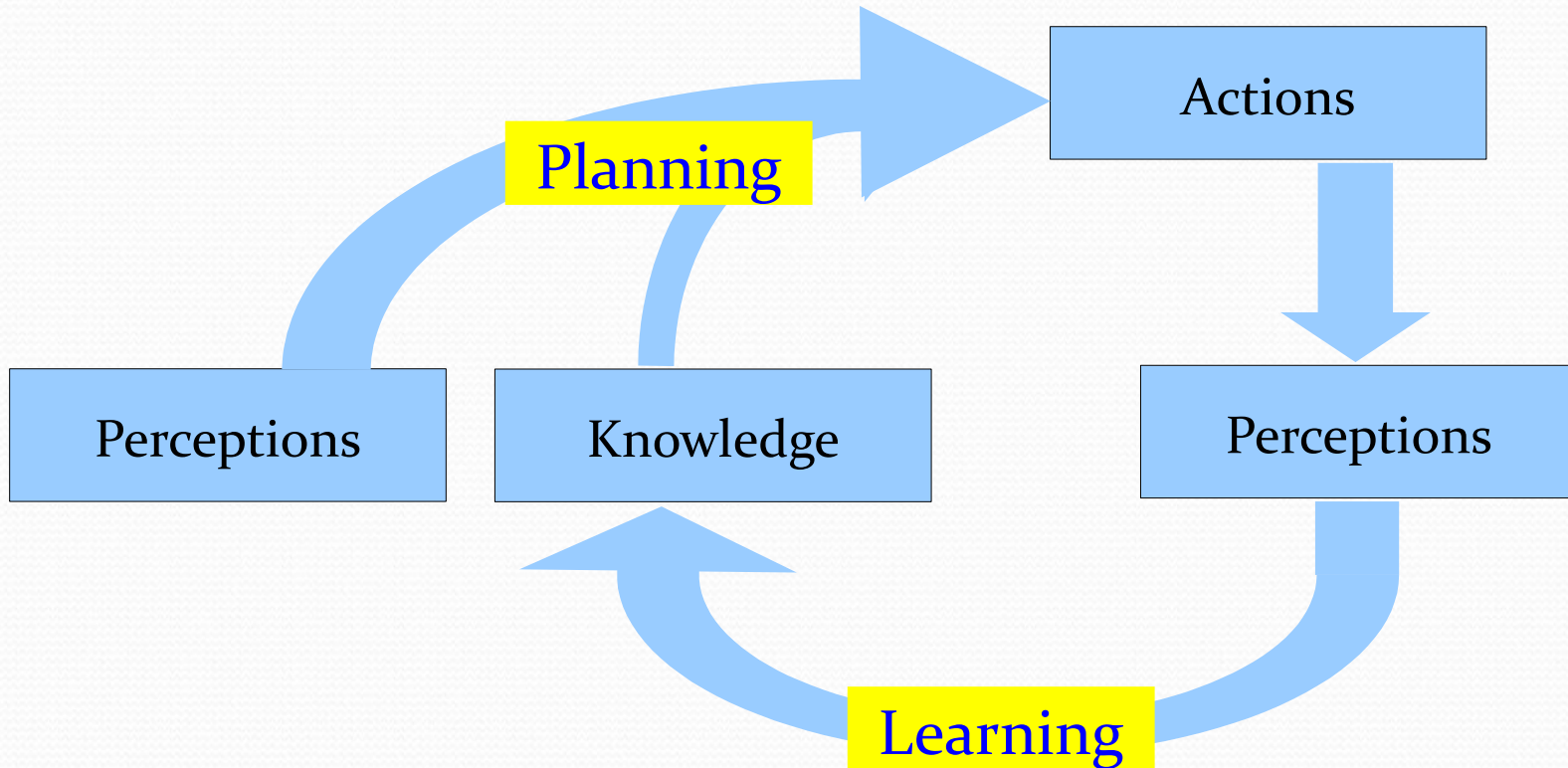
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# Artificial Intelligence

- Aims to develop intelligent agents that perceive their environment and take actions that maximize their chances of success
- Requires solving several challenges:
  - Knowledge representation:  
how does an agent represent its knowledge and perceptions?
  - Reasoning, planning:  
how does an agent deduce an action based on its perceptions and its knowledge?
  - Learning:  
how does an agent update its knowledge based on its perceptions?

# Artificial Intelligence



# Computational Intelligence

- Computational intelligence traditionally studies a subset of three AI techniques:
  - Knowledge representation:  
fuzzy logic & fuzzy set theory
  - Reasoning, planning:  
Evolutionary (genetic) algorithms
  - Learning:  
Neural networks

# Knowledge representation: Fuzzy logic

- **Goal:**  
represent “fuzzy” knowledge of an agent
- Traditional logic can be used to represent crisp rules:

*if A is true then do B*

Boolean in → Boolean out

- Fuzzy logic represents fuzzy rules:

*if A is true to a high degree / A is likely then try to make B true to a high degree / make B likely*

Number in → Number out

**Fuzzy logic is less sensitive to errors / noise**

# Knowledge representation: Fuzzy logic

- Used to build control systems

*if A is warm to a high degree then B should be turned down to a high degree*

- Used to calculate the overall quality (fitness) of a (hypothetical) situation

*if A is high then customer is likely good*

*if B is high then customer is likely good*

*if C is high and B is not high then customer is likely good*

how good would the situation be in which A and C are high, and B is low?

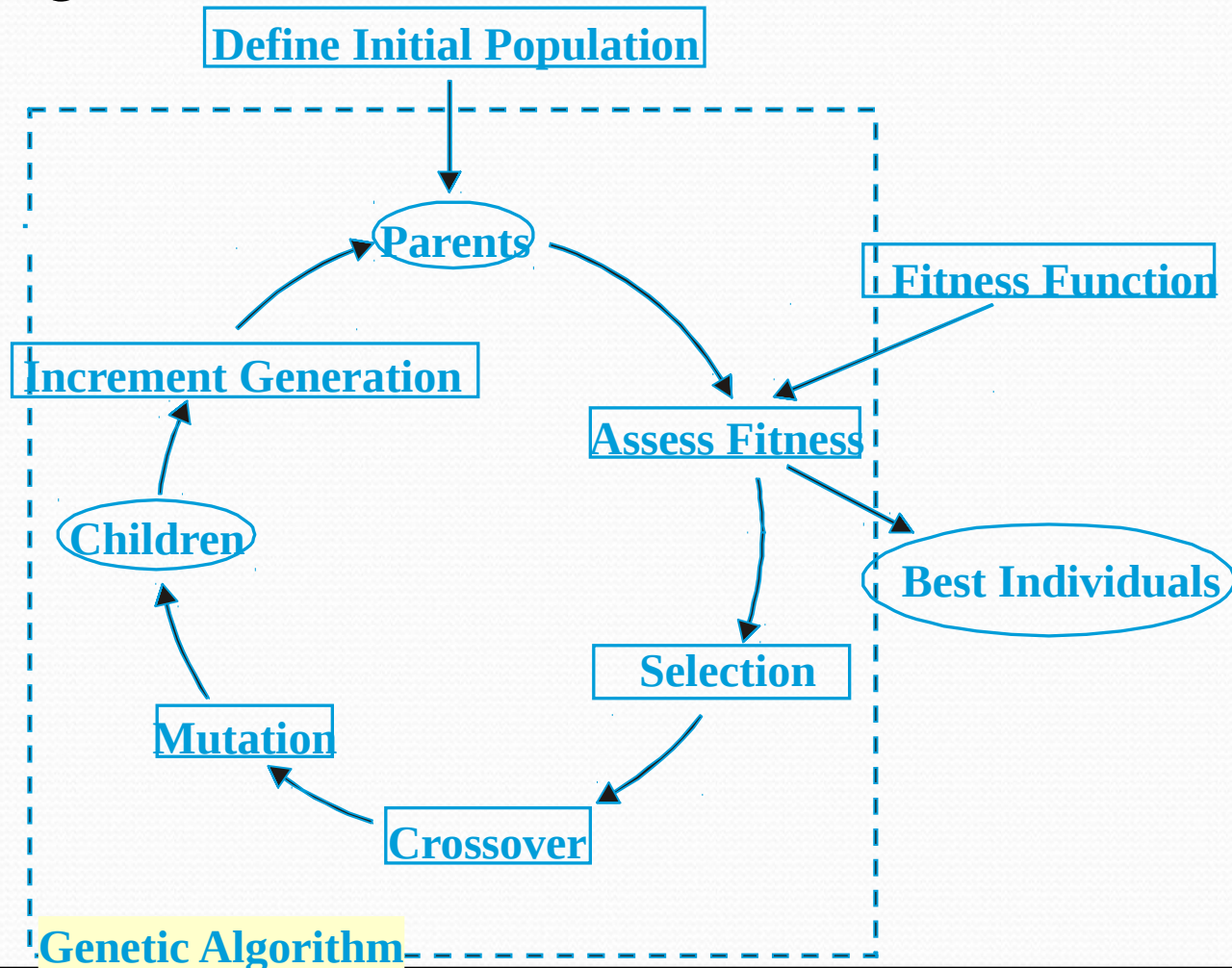
- ***Research challenges: how to interpret fuzzy rules? What are sensible strategies for calculating an output, given inputs? How to make the intuition formal?***

# Planning / optimization: Evolutionary Algorithms

- **Goal of an evolutionary algorithm:**  
to find a plan that optimizes a given fitness function
  - the fitness could be defined by means of fuzzy logic, but does not have to be
- **Example:**  
the traveling salesman problem
  - **Given** a number of cities, distances between the cities
  - **Find** an order in which to visit the cities such that the total distance traveled is minimized

# Evolutionary Algorithms

- **Method:** evolve populations of solutions by mimicking evolution in nature





# Nature-inspired optimization

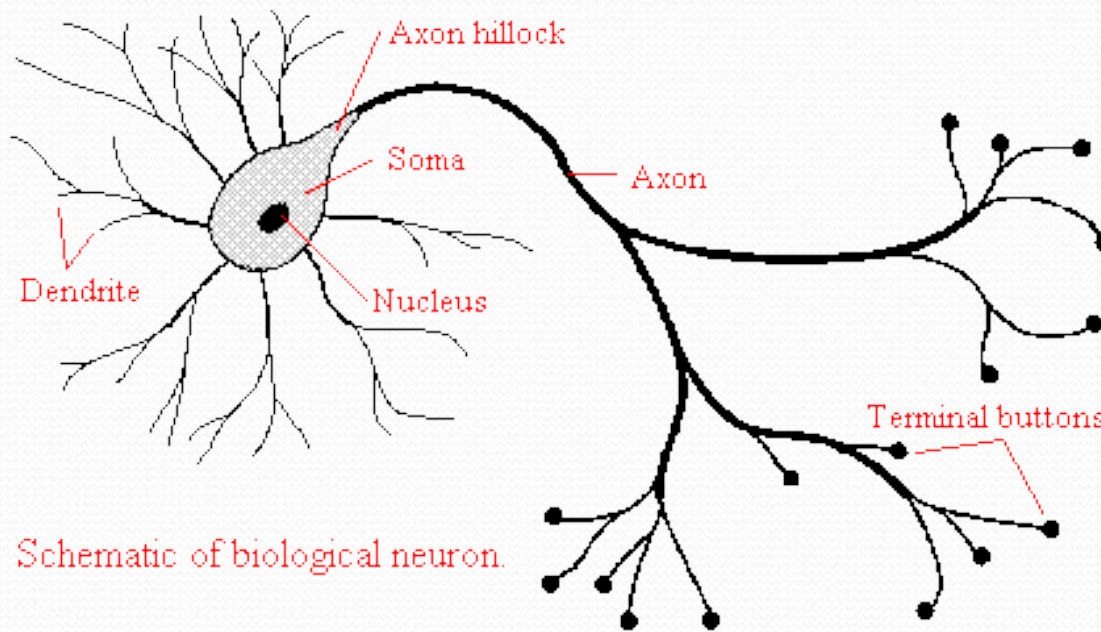
- Evolutionary algorithms
- Particle swarm optimization
- Artificial ants

**All are  
robust optimization algorithms:  
if the fitness function changes, solutions usually adapt  
relatively easily**

- **Research challenge: which algorithm finds a good solution as quickly as possible?**

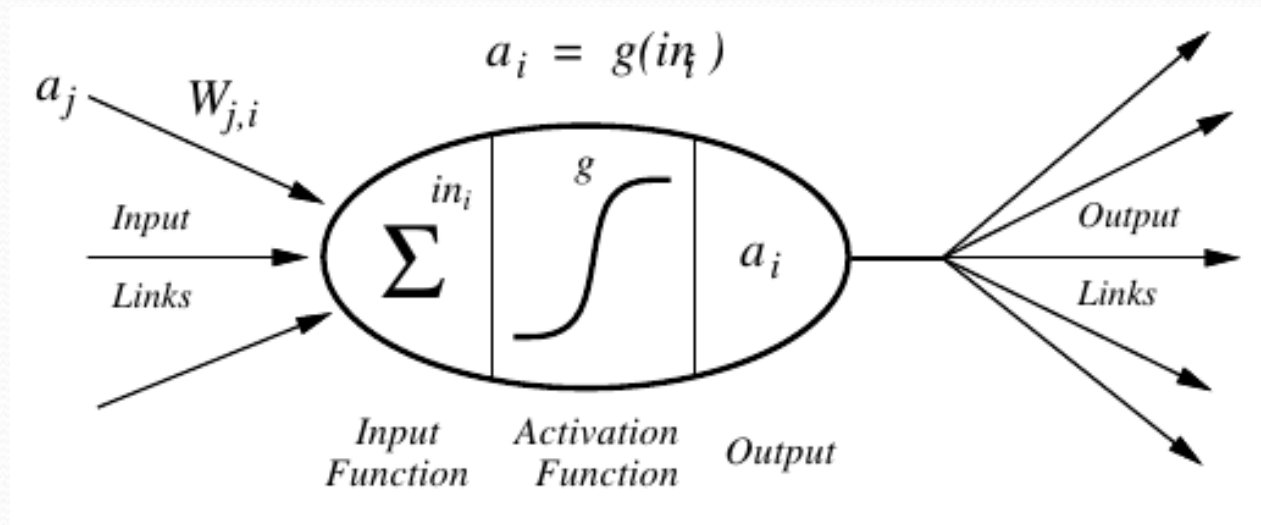
# Learning: Neural Networks

- Inspired by biological nervous systems



# Learning: Neural Networks

- Artificial neuron



*(Neuron/Unit)*

- Also a neural network represents knowledge, and is often used used to transform input to output

# Learning:

## Neural Networks

- Different types of neural networks:
  - feed-forward neural networks
  - self-organizing maps
  - recurrent networks
  - radial basis function networks
  - fuzzy-neural networks

**Research challenge: how to learn a neural network?  
What is a good architecture for a neural network?**

# Computational Intelligence

- Knowledge representation: fuzzy logic & fuzzy set theory → You haven't followed a basic course on logic
- Reasoning, planning: Evolutionary (genetic) algorithms
- Learning: Neural networks → Basis already discussed in course artificial intelligence
  - Also in course on data mining
  - Advanced topics require strong mathematics

● Knowledge representation & planning:  
traditional logic, SAT solvers, constraint programming

# Computational Intelligence

● Knowledge representation:  
fuzzy logic & fuzzy set theory

● Reasoning, planning:  
Evolutionary (genetic) algorithms

~~● Learning:  
Neural networks~~

# Central Theme

- Artificial intelligence inspired methods for
  - Knowledge representation:
    - Logic
    - Fuzzy logic
  - Optimization & planning:
    - SAT solving
    - Constraint programming
    - Local search
    - Evolutionary algorithms
- Problems related to *operations research*

# Template of a Constraint Optimization Problem

- **Given:**
  - ...
- **Find:**
  - ...
- **Such that:**
  - ... is **minimal/maximal**
  - ... is satisfied



# Example 1: Traveling Salesmen

- **Given:**

- $N$  cities
- $D[i,j]$  distances between cities

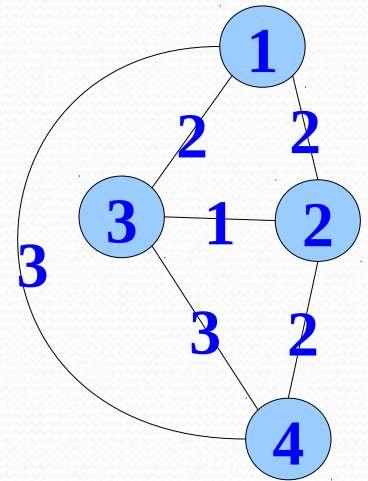
- **Find:**

- an assignment  $p[i]$  for  $i=1..N$  with  $p[i]$  in  $1..N$ , indicating that at step  $i$  city  $p[i]$  is visited

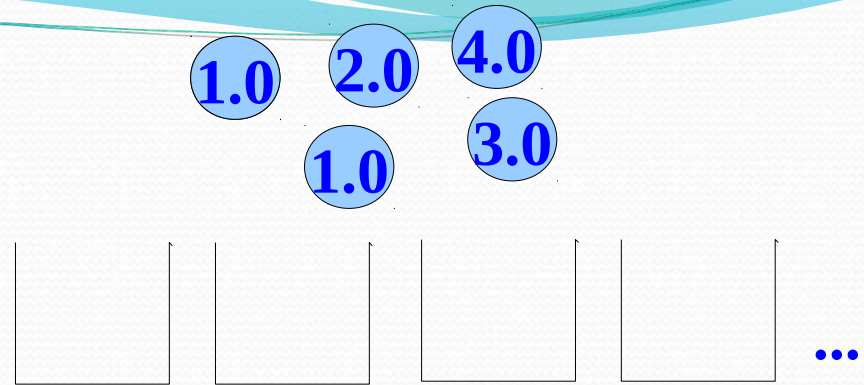
- **Such that:**

- all cities are visited exactly once
- $D[p[1],p[2]]+D[p[2],p[3]]+\dots+D[p[n-1],p[n]]+D[p[n],p[1]]$  is **minimal**

Optimization



# Example 2: Binpacking



- **Given:**

- $N$  items with sizes  $a_1, \dots, a_N$
- A bin size  $V$

**Each bin: 4.0**

- **Find:**

- an assignment  $p[i]$  for  $i=1..N$  to positive integers, indicating that item  $i$  is put in bin  $p[i]$

- **Such that:**

- $\max_i p[i]$  is **minimal** (number of bins is small)
- $\sum_{p[i]=j} a_i \leq V$  for all bins  $j$  (no more than weight  $V$  in each bin)

# Example 3: Knapsack

- **Given:**

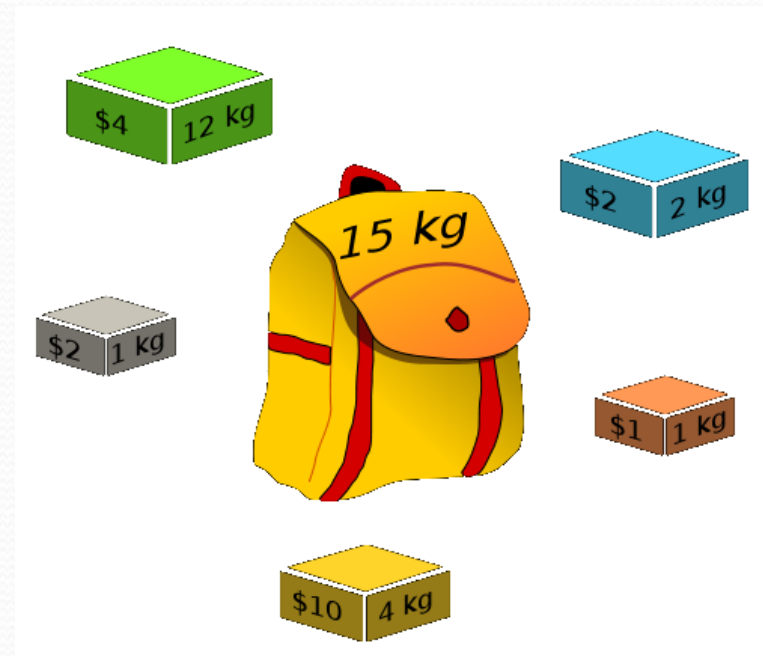
- $N$  items with sizes  $a_1, \dots, a_N$ , prices  $p_1, \dots, p_N$
- A maximum weight  $W$

- **Find:**

- a subset of items  $I$

- **Such that:**

- $\sum_{i \in I} p_i$  is **maximal** (very valuable knapsack)
- $\sum_{i \in I} a_i \leq W$  (knapsack with low weight)



# Example 3b:

## Unbounded Knapsack

- **Given:**

- $N$  possible items with weights  $a_1, \dots, a_N$ , prices  $p_1, \dots, p_N$
- A weight threshold  $W$

- **Find:**

- an integer  $w[i]$  for each item  $i$

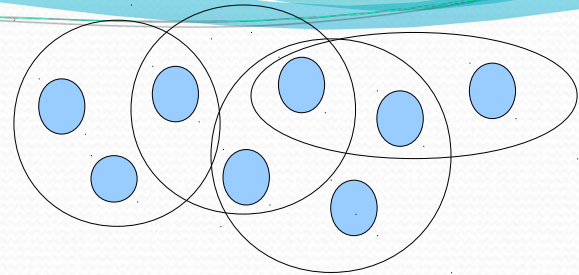
- **Such that:**

- $\sum_{i=1}^N w[i]p_i$  is **maximal** (very valuable knapsack)
- $\sum_{i=1}^N w[i]a_i \leq W$  (knapsack with low weight)

**Portfolio  
Optimization**

# Example 4:

## Set Cover



- **Given:**

- $N$  sets, each a subset of the universe  $U = \{1, 2, \dots, m\}$

- **Find:**

- A subset  $S$  of the  $N$  given sets, i.e. each set in  $S$  equals one of the given sets, but not all given sets need to be selected.

- **Such that:**

- $|S|$  is **minimal** (small subset)

- $\bigcup_{S \in S} S = U$  (each element is covered)

# Decision vs Optimization Problems

- Optimization problem:
  - Find ...
  - Such that:
    - $f(\dots)$  is minimal
    - constraints are satisfied
- Decision problem:
  - Find ...
  - Such that:
    - $f(\dots) < \textit{threshold}$
    - constraints are satisfied
- Optimization problems over finite domains can be turned into repeated decision problems: iterate over possible thresholds

# How to solve these problems?

- Many such problems are hard
  - “NP hard” → no polynomial algorithm is known
- Two solutions:
  - Exact: require exponential time in the worst case
  - Inexact: polynomial, but may not find the best solutions
- Both types of solutions have been studied in artificial intelligence, algorithms, and operations research

# High-Level, Declarative Problem Solving in AI

- Distinguishing feature of AI approaches: they aim to be “intelligent” and generic by solving problems (semi-)automatically
- Idea: solve a problem in two stages:
  - 1. Describe the problem in a concise way in a computer language.
  - 2. Run a general algorithm (a “solver” or an “inference engine”) on this description to solve the problem.

i.e., the programmer does **not** write an imperative algorithm.



# High-Level Declarative Problem Solving in AI

- Example search: evolutionary algorithm
  - Step 1:
    - Specify what the individuals in a population look like
    - Specify the quality of an individual (fitness)
  - Step 2: (Ideal situation)
    - Run an existing evolutionary algorithm without modification



**Evolutionary  
Algorithm**

**Black box**

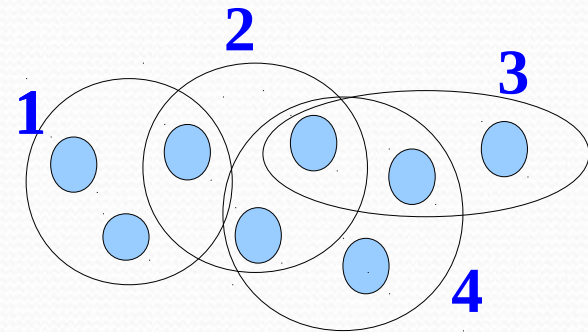
# High-Level Declarative Problem Solving in AI

- Example problem: set cover
- Representation of an individual in a bitstring:



**2<sup>nd</sup> and 3<sup>rd</sup> set are selected**

- Fitness: (assuming small=very fit)
  - Number of sets selected?
  - Number of sets selected + ( number of uncovered elements )  $\times w$



**Very large weight**

# High-Level Declarative Problem Solving in AI

- What about optimal solutions?
- Alternative *general* systems that take a *declarative* input specification and find optimal solutions:
  - Constraint programming
  - SAT solvers
  - ILP solver

# High-Level Declarative Problem Solving in AI

- Which programming language to use?
  - C++ ?
  - Java ?
  - Prolog ?
  - Python

# Why Python?

- Scripting language with a high level of abstraction
  - Implements features also seen in functional and logic programming
- Well-supported language with many libraries available
- Quickly gaining popularity in the scientific community (Coursera)

# Why Python?











| Language Rank | Types  | 2015<br>Spectrum Ranking | 2014<br>Spectrum Ranking |
|---------------|--------|--------------------------|--------------------------|
| 1. Java       | 🌐 📱 🖥️ | 100.0                    | 100.0                    |
| 2. C          | 📱 🖥️ 🧠 | 99.9                     | 99.3                     |
| 3. C++        | 📱 🖥️ 🧠 | 99.4                     | 95.5                     |
| 4. Python     | 🌐 🖥️   | 96.5                     | 93.5                     |
| 5. C#         | 🌐 📱 🖥️ | 91.3                     | 92.4                     |
| 6. R          | 🖥️     | 84.8                     | 84.8                     |
| 7. PHP        | 🌐      | 84.5                     | 84.5                     |
| 8. JavaScript | 🌐 📱    | 83.0                     | 78.9                     |
| 9. Ruby       | 🌐 🖥️   | 76.2                     | 74.3                     |
| 10. Matlab    | 🖥️     | 72.4                     | 72.8                     |

(IEEE Spectrum)

# Why Python?

2016

2015

| Language Rank | Types   | Spectrum Ranking | Custom Ranking |
|---------------|---|------------------|----------------|
| 1. C          |    | 100.0            | 100.0          |
| 2. Java       |    | 98.1             | 99.7           |
| 3. Python     |    | 98.0             | 99.1           |
| 4. C++        |    | 95.9             | 95.8           |
| 5. R          |    | 87.9             | 91.0           |
| 6. C#         |    | 86.7             | 84.1           |
| 7. PHP        |    | 82.8             | 83.6           |
| 8. JavaScript |  | 82.2             | 82.6           |
| 9. Ruby       |  | 74.5             | 74.8           |
| 10. Go        |  | 71.9             | 73.3           |

# Computational Intelligence

- Basic course in Python
- Knowledge representation & planning:  
traditional logic, **SAT solvers, constraint programming**
- Knowledge representation:  
fuzzy logic & fuzzy set theory
- Reasoning, planning:  
Evolutionary (genetic) algorithms
- ~~● Learning:  
Neural networks~~



# Course overview

- Lectures & practicums will often be combined

@Snellius

Informatica & Economie Derde jaar najaar 2016-2017, BIS

| wk nr | Datum Ma | Maandag        |   |      |        |   |   |       |   | Dinsdag  |   |     |       |      |   |   |   | Woensdag |     |   |   |   |          |          |   | Donderdag |     |     |   |      |     |   |   | Vrijdag |        |     |   |   |   |    |     |
|-------|----------|----------------|---|------|--------|---|---|-------|---|----------|---|-----|-------|------|---|---|---|----------|-----|---|---|---|----------|----------|---|-----------|-----|-----|---|------|-----|---|---|---------|--------|-----|---|---|---|----|-----|
|       |          | 1              | 2 | 3    | 4      | 5 | 6 | 7     | 8 | 1        | 2 | 3   | 4     | 5    | 6 | 7 | 8 | 1        | 2   | 3 | 4 | 5 | 6        | 7        | 8 | 1         | 2   | 3   | 4 | 5    | 6   | 7 | 8 | 1       | 2      | 3   | 4 | 5 | 6 | 7  | 8   |
| 36    | 5 sep    |                |   | HCI* |        |   |   |       |   |          |   |     | SBIS  |      |   |   |   |          |     |   |   |   | CI       | pCI      |   |           |     | HCI |   | CI   | pCI |   |   |         |        |     |   |   |   |    |     |
| 37    | 12 sep   |                |   |      | DaMi   |   |   |       |   |          |   |     | SBIS  |      |   |   |   |          |     |   |   |   | CI       | pCI      |   |           |     | HCI |   |      |     |   |   |         |        |     |   |   |   | CI | pCI |
| 38    | 19 sep   |                |   | HCI  | DaMi   |   |   |       |   |          |   |     | SBIS  |      |   |   |   |          |     |   |   |   | CI       | pCI      |   |           |     | HCI |   |      |     |   |   |         |        |     |   |   |   | CI | pCI |
| 39    | 26 sep   |                |   | HCI  | DaMi   |   |   |       |   |          |   |     | SBIS  |      |   |   |   |          |     |   |   |   | CI       | pCI      |   |           |     | HCI |   |      |     |   |   |         |        |     |   |   |   | CI | pCI |
| 40    | 3 okt    | Leidens Ontzet |   |      |        |   |   |       |   |          |   |     |       | SBIS |   |   |   |          |     |   |   |   | CI       | pCI      |   |           |     | HCI |   |      |     |   |   |         |        |     |   |   |   | CI | pCI |
| 41    | 10 okt   |                |   | HCI  | DaMi   |   |   |       |   |          |   |     | SBIS  |      |   |   |   |          |     |   |   |   | CI       | pCI      |   |           |     | HCI |   |      |     |   |   |         |        |     |   |   |   | CI | pCI |
| 42    | 17 okt   |                |   | HCI  | DaMi   |   |   |       |   |          |   |     | SBIS  |      |   |   |   |          |     |   |   |   | CI       | pCI      |   |           |     | HCI |   |      |     |   |   |         |        |     |   |   |   | CI | pCI |
| 43    | 24 okt   |                |   | HCI  | DaMi   |   |   |       |   |          |   | Fin |       |      |   |   |   |          | Fin |   |   |   |          |          |   |           | HCI |     |   |      |     |   |   |         | Fin pr | Fin |   |   |   |    |     |
| 44    | 31 okt   |                |   | HCI  | DaMi   |   |   | t Fin |   |          |   | Fin |       |      |   |   |   |          | Fin |   |   |   |          | CI/pr CI |   |           | HCI |     |   |      |     |   |   |         | Fin pr | Fin |   |   |   |    |     |
| 45    | 7 nov    |                |   | HCI  | DaMi   |   |   | t Fin |   |          |   | Fin |       |      |   |   |   |          | Fin |   |   |   |          | CI/pr CI |   |           | HCI |     |   |      |     |   |   |         | Fin pr | Fin |   |   |   |    |     |
| 46    | 14 nov   |                |   | HCI  | DaMi   |   |   | t Fin |   |          |   | Fin |       |      |   |   |   |          | Fin |   |   |   |          | CI/pr CI |   |           | HCI |     |   |      |     |   |   |         | Fin pr | Fin |   |   |   |    |     |
| 47    | 21 nov   |                |   | HCI  | DaMi   |   |   | t Fin |   |          |   | Fin | Bach  |      |   |   |   | Fin      |     |   |   |   | CI/pr CI |          |   | HCI       |     |     |   |      |     |   |   | Fin pr  | Fin    |     |   |   |   |    |     |
| 48    | 28 nov   |                |   | HCI  | DaMi   |   |   | t Fin |   |          |   | Fin |       |      |   |   |   | Fin      |     |   |   |   | CI/pr CI |          |   | HCI       |     |     |   |      |     |   |   | Fin pr  | Fin    |     |   |   |   |    |     |
| 49    | 5 dec    |                |   | HCI  | DaMi   |   |   | t Fin |   |          |   | Fin | Bach  |      |   |   |   | Fin      |     |   |   |   | CI/pr CI |          |   | HCI       |     |     |   |      |     |   |   | Fin pr  | Fin    |     |   |   |   |    |     |
| 50    | 12 dec   |                |   |      | DaMi   |   |   |       |   |          |   | Fin | T Fin |      |   |   |   | Fin      |     |   |   |   | CI/pr CI |          |   | HCI       |     |     |   | T CI |     |   |   | Fin pr  | Fin    |     |   |   |   |    |     |
| 51    | 19 dec   | Gesloten       |   |      |        |   |   |       |   | Gesloten |   |     |       |      |   |   |   | Gesloten |     |   |   |   |          |          |   | Gesloten  |     |     |   |      |     |   |   |         |        |     |   |   |   |    |     |
| 1     | 2 jan    |                |   |      | T HCI  |   |   |       |   |          |   |     |       |      |   |   |   |          |     |   |   |   |          |          |   |           |     |     |   |      |     |   |   |         |        |     |   |   |   |    |     |
| 2     | 9 jan    |                |   |      | T DaMi |   |   |       |   |          |   |     |       |      |   |   |   |          |     |   |   |   |          |          |   |           |     |     |   |      |     |   |   |         |        |     |   |   |   |    |     |
| 3     | 16 jan   |                |   |      |        |   |   |       |   |          |   | HCI | Bach  |      |   |   |   |          |     |   |   |   |          |          |   |           |     |     |   |      |     |   |   |         |        |     |   |   |   |    |     |
| 4     | 23 jan   |                |   |      |        |   |   |       |   |          |   |     | Bach  |      |   |   |   |          |     |   |   |   |          |          |   |           |     |     |   |      |     |   |   |         |        |     |   |   |   |    |     |
| 4     | 25 jan   |                |   |      |        |   |   |       |   |          |   |     | Bach  |      |   |   |   |          |     |   |   |   |          |          |   |           |     |     |   |      |     |   |   |         |        |     |   |   |   |    |     |

- Final mark obtained 70% from a written exam and 30% from practicum assignments
- [Http://www.liacs.leidenuniv.nl/~nijssensgr/CI/](http://www.liacs.leidenuniv.nl/~nijssensgr/CI/)